



**SECTION – B**  
**(Short-Answer Questions – Marks 50)**

Note: Attempt any TEN part questions from this section, selecting at least THREE part questions from each question. You may choose the tenth part question from any one sub-section. All questions carry equation marks.

**COMPLEX NUMBER, MATRIX AND DETERMINANT, VECTORS AND FUNCTION & GRAPHS**

- Q. 2. i). Solve the quadratic equation  $z^2 - 6z = -13$  by completing the squares, where  $z$  is a complex number.
- ii). Find the period of the following period matrix.
- $$\begin{bmatrix} 1 & -2 & -6 \\ -3 & 2 & 9 \\ 2 & 0 & -3 \end{bmatrix}$$
- iii). Without expanding determinants, prove that.
- $$\begin{vmatrix} \alpha & \beta\gamma & \alpha\beta\gamma \\ \beta & \gamma\alpha & \alpha\beta\gamma \\ \gamma & \alpha\beta & \alpha\beta\gamma \end{vmatrix} = \begin{vmatrix} \alpha & \alpha^2 & \alpha^3 \\ \beta & \beta^2 & \beta^3 \\ \gamma & \gamma^2 & \gamma^3 \end{vmatrix}$$
- iv). A force of  $22N$  is applied to the end of  $0.15$  meter wrench at an angle of  $75$  degrees with the axis of rotation. Calculate the magnitude of the moment  $\vec{M}_o$  produced by applied force.
- v). Find the point of intersection of the following function graphically.
- $$f(x) = x + 2 \quad \text{and} \quad g(x) = x^2 - 4x + 6$$

**SEQUENCE & SERIES, PROBABILITY, MATHEMATICAL INDUCTION & BINOMIAL THEOREM**

- Q. 3. i). If the  $p$ th term of an H. P. is  $q$ , the  $q$ th term is  $p$ ; prove that the  $(p + q)$ th term is  $\frac{pq}{(p+q)}$ .
- ii). Find the sum of the following series.  $3 + 6 + 21 + 96 + 471 + \dots$  to  $n$  terms
- iii). How many words can be formed by 3 vowels and 4 consonants out of 5 vowels and 7 consonants.
- iv). If the probability of solving a problem by two students Ahsan and Umar are  $\frac{1}{2}$  and  $\frac{1}{3}$  respectively then what is the probability of the problem to be solved.
- v). Prove the following statemen by mathematical induction.  $7^n - 4^n$  is divisible by 3.

**LINEAR PROGRAMING AND TRIGONOMETRY**

- Q. 4. i). Solve the following LP programming problems by graphical method when  $x \geq 0, y \geq 0$ .  
Maximize the objective function  $z = f(x, y) = 10x + 11y$ ,  
Subject to the constraints  $2x + 3y \leq 8; 6x + 3y \leq 10$ .
- ii). Express  $4 \sin \theta + 3 \cos \theta$  in the form  $r \sin(\theta + \varphi)$ , where  $\theta$  and  $\varphi$  are in first quadrant.
- iii). Prove that. (a).  $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$   
(b).  $\frac{\sin 6\theta + \sin 4\theta}{\cos 6\theta + \cos 4\theta} = \tan 5\theta$
- iv). The area of triangle is  $3.346$  square unit. If  $\beta = 20.9^\circ, \gamma = 117.2^\circ$ . Find  $a$  and angle  $\alpha$ .
- v). Solve the equation  $\cos \theta - \theta = 0$ , graphically for the interval  $-\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$ .

**SECTION – C**  
**(Detailed-Answer Questions – Marks 30)**

Note: Attempt any TWO questions. All questions carry equal marks.

- Q. 5. a). Solve the non-homogeneous system of linear equations using Gauss Jordan method.  
 $2x + 2y - z = 4$                        $x - 2y + z = 2$                        $x + y = 0$                       (Marks 08)
- b). Find the volume of the tetrahedron whose vertices are  $A(2, 1, 8)$ ,  $B(3, 2, 9)$ ,  $C(2, 1, 4)$ , and  $D(3, 3, 10)$ . (Marks 07)
- Q. 6. a). If  $x = \frac{1}{3} + \frac{1.3}{3.6} + \frac{1.3.6}{3.6.9} + \frac{1.3.6.9}{3.6.9.12} + \dots$ , prove that  $x^2 + 2x - 2 = 0$ . (Marks 08)
- b). The starting salary of a peon was Rs.8000/= and after each subsequent year his salary was increased by 15%. What total amount of salary he got for the first twelve years? (Marks 07)
- Q. 7. a). Find and verify the general solution of the following trigonometric equation. (Marks 08)  
$$3 \tan^2 x + 2\sqrt{3} \tan x = -1$$
- b). The sides of a parallelogram are 25cm and 35cm long and one of its angles is  $36^\circ$ . Find the lengths of its diagonals. (Marks 07)

**Good Luck**

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